

Sections 7.1 – 7.3 I.C.E

Name: _____

For 1 – 4, solve the system algebraically (Substitution or Elimination).

1) $x + 2y = 1$
 $5x - 4y = -23$

2) $x - y = 3$
 $x - y^2 = 1$

3) $2x - y + 3 = 0$
 $x^2 + y^2 - 4x = 0$

4) $2x + y - z = 7$
 $x - 2y + 2z = -9$
 $3x - y + z = 5$

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You can choose any method to solve the problems below- just define your variables, set up two or three equations, and then solve by the method of your choosing.

- 5) A total of \$32,000 is invested in two municipal bonds that pay 5.75% and 6.25% simple interest. The investor wants an annual interest income of \$1900 from the investments. How much should be invested in each type of bond?

- 6) Two planes start from LA International Airport and fly in opposite directions. The second plane starts one half hour after the first plane, but its speed is 80 km/hr faster. Find the airspeed of each plane if 2 hours after the first plane departs, the planes are 3200 km apart.

- 7) What are the dimensions of a rectangular tract of land if its perimeter is 40 kilometers and its area is 96 square kilometers?

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- 8) Ten liters of a 30% acid solution is obtained by mixing a 20% solution with a 50% solution. How much of each solution is required to obtain the specified concentration of the final mixture?
- 9) In Super Bowl I, the Green Bay Packers defeated the Kansas City Chiefs by a score of 35 to 10. The total points scored came from 13 different scoring plays, which were a combination of touchdowns, extra-point kicks, and field goals, worth 6, 1, and 3 points respectively. The same number of touchdowns and extra point kicks were scored. There were six times as many touchdowns as field goals. How many touchdowns, extra-point kicks, and field goals were scored during the game?

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Solutions!

ICE 7.1-7.3

1. $(-3, 2)$
2. $(5, 2)$ and $(2, -1)$
3. no solution
4. no solution
5. \$20,000 at 5.75%
\$12,000 at 6.25%

6. F = first plane's speed, S = second plane's speed

$$\begin{aligned} \text{Distance} &= \text{rate} \times \text{time} & F &= S - 80 \\ 3200 &= (F) \times \text{time} + (S) \times \text{time} \\ 3200 &= (S - 80) \times 2 \text{ hrs} + S \times 1.5 \text{ hrs} \\ 3200 &= (2S - 160 + 1.5S) \\ 1600 &= 1.5S - 160 \\ 1760 &= 1.5S \\ S &= 960 \end{aligned}$$

the second plane's speed is 960 km/hr, and the first plane's speed is 880 km/hr

7. $2b + 2h = 40 \rightarrow b = 20 - h$

$$\begin{aligned} bh &= 96 & \rightarrow (20 - h)h &= 96 \\ 20h - h^2 &= 96 \\ h^2 - 20h + 96 &= 0 \\ (h - 8)(h - 12) &= 0 \\ h &= 8 \text{ or } h = 12 \rightarrow \text{dimensions are } 8\text{km} \times 12\text{km} \end{aligned}$$

8. $.50x + .20y = .30$ (10)

$$\begin{aligned} x + y &= 10 \rightarrow x = 10 - y \\ .50(10 - y) + .20y &= 3 \\ 5 - .50y + .20y &= 3 \\ -.30y &= -2 \rightarrow y = 20/3 \text{ liters, so } x = 10/3 \text{ liters} \end{aligned}$$

9. $T + E + F = 13 \rightarrow T + T + F = 13$ or $6F + 6F + F = 13$

$$6T + E + 3F = 45$$

$$13F = 13$$

$$T = E$$

$$F = 1 \rightarrow T = 6 \rightarrow E = 6$$

$$6F = T$$

There were 6 touchdowns and extra points, and 1 field goal