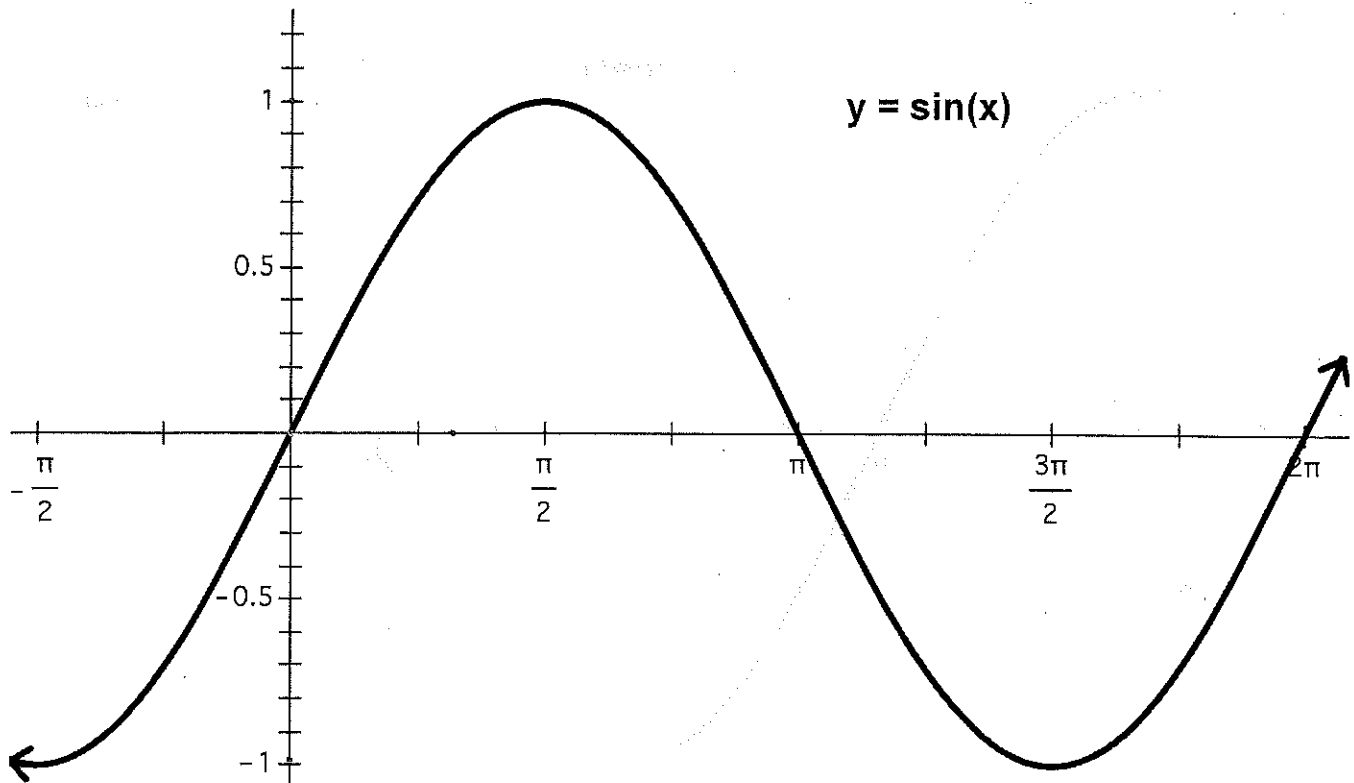


Sections 4.5 – Graphs of Sine & Cosine Functions

Sine Curve

****The graph of the sine function****

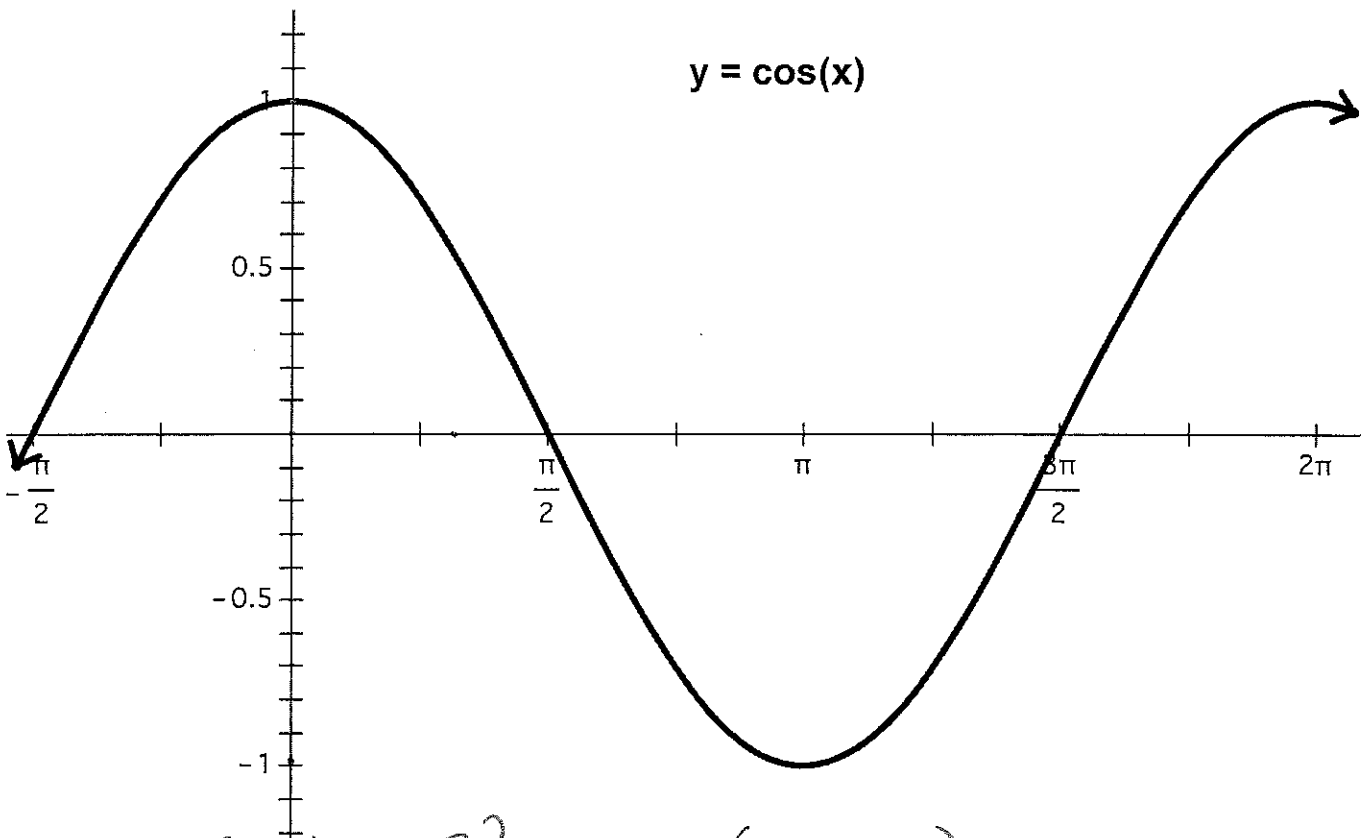


- Domain: $\{x \mid x \in \mathbb{R}\}$ or $(-\infty, \infty)$
- Range: $\{y \mid -1 \leq y \leq 1\}$ or $[-1, 1]$
- Symmetric with respect to the **origin** so this is an **ODD** function.
- Period: 2π
- Zeros: $\dots, -\pi, 0, \pi, 2\pi, \dots$
- Max: 1
- Min: -1

Sections 4.5 – Graphs of Sine & Cosine Functions

Cosine Curve

****The graph of the cosine function****



- Domain: $\{x \mid x \in \mathbb{R}\}$ or $(-\infty, \infty)$
- Range: $\{y \mid -1 \leq y \leq 1\}$ or $[-1, 1]$
- Symmetric with respect to they-axis so an **EVEN** function
- Period: 2π
- Zeros: $\dots, -\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{2}, \dots$
- Max: 1
- Min: -1

Sections 4.5 – Graphs of Sine & Cosine Functions

Important Vocab

Amplitude – *half the distance between the minimum and maximum value of a function over a given range.*

Period – *the distance required to complete one full cycle (one complete repetition of a pattern)*

Frequency – *the number of cycles completed in a given interval (frequency = $\frac{1}{\text{period}}$)*

Summary of Translations of Sine and Cosine

$$Y = A \sin B(x - C) + D$$

$$A = \text{amplitude}$$

$$B = \text{frequency} \text{ which gives us a period of } \frac{2\pi}{B}$$

$$C = \text{Horizontal shift}$$

$$D = \text{Vertical shift}$$

The general equations,

$$y = A \sin B(x - C) + D$$

and

$$y = A \cos B(x - C) + D$$

have the following characteristics:

$$\text{amplitude} = |A|$$

$$\text{period} = \frac{2\pi}{B}$$

1. If $C > 0$ there is a horizontal shift C units to the right
if $C < 0$ there is a horizontal shift C units to the left.
2. If $D > 0$ the shift is D units upward
if $D < 0$ the shift is D units downward.
3. If $A < 0 \rightarrow$ reflection across x -axis.
4. If $B < 0 \rightarrow$ reflection across y -axis.

Sections 4.5 – Graphs of Sine & Cosine Functions

Examples:

Describe the change (transformations) between the following graphs and their respective parent functions- consider amplitude, period and shifts:

a) $y = -4\cos(5x)$

amplitude: 4

period: $2\pi/5$

Reflection? X-axis

Shifts: none

b) $y = \frac{1}{2}\sin(6x)$

amplitude: $\frac{1}{2}$

period: $\pi/3$

Reflection? none

Shifts: none

c) $f(x) = -3\sin(x+\pi)$

amplitude: 3

period: 2π

Reflection? X-axis

Shifts: Left by π

d) $f(x) = \cos\frac{1}{4}x + 8$

amplitude: 1

period: $2\pi/1/4 = 8\pi$

Reflection? none

Shifts: up 8

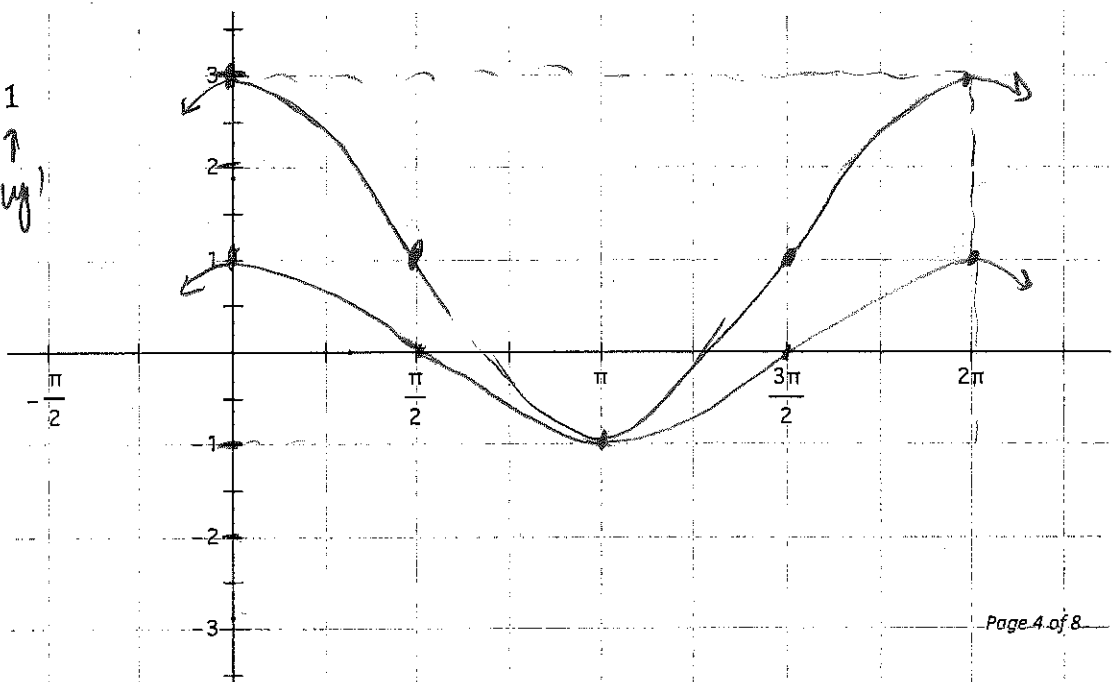
Graph the following functions:

a) $y = \cos x$

b) $y = 2\cos x + 1$

\uparrow
amp

\uparrow
 y'



Sections 4.5 – Graphs of Sine & Cosine Functions

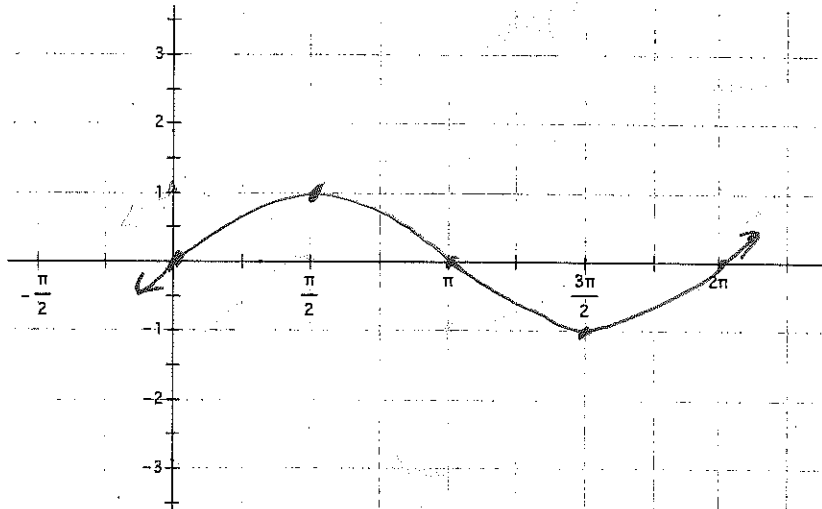
More Examples!

For the following graphs, graph on the same coordinate axes.

You should graph at least between 0 and 2π , unless you want to graph more...

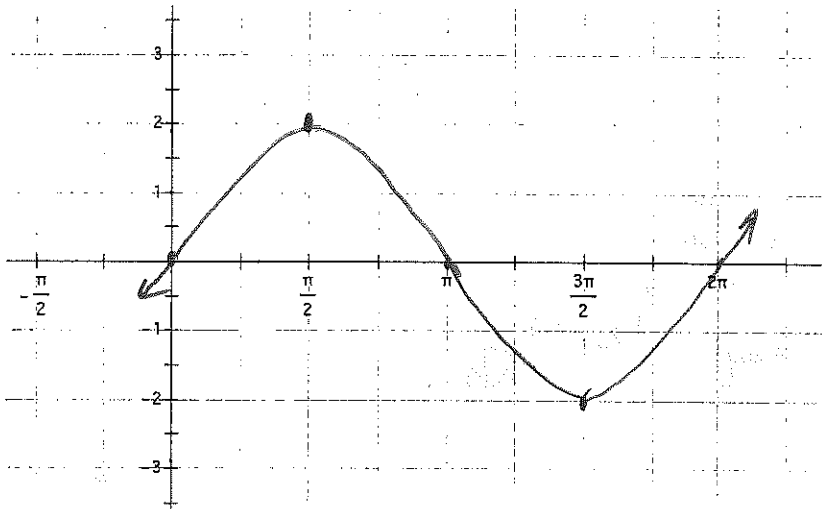
1.

a) $y = \sin x$



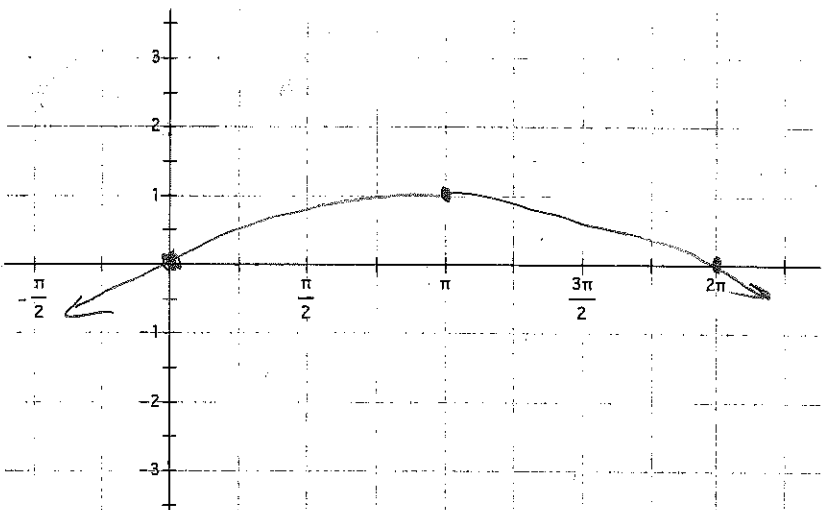
b) $y = 2\sin x$

↑
ampl = 2



c) $y = \sin\left(\frac{1}{2}x\right)$

↑
period =
 $\frac{2\pi}{1/2} = 4\pi$



Sections 4.5 – Graphs of Sine & Cosine Functions

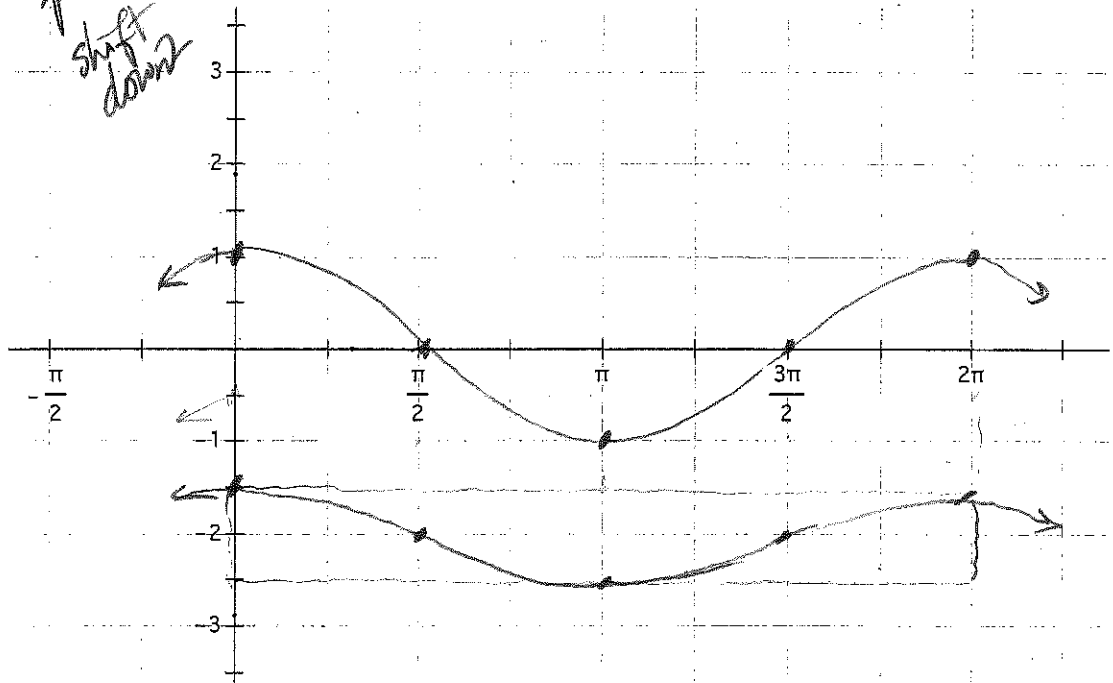
2.

a) $y = \cos x$

b) $y = \frac{1}{2} \cos x - 2$

↑
amp = $\frac{1}{2}$

↑
shift down



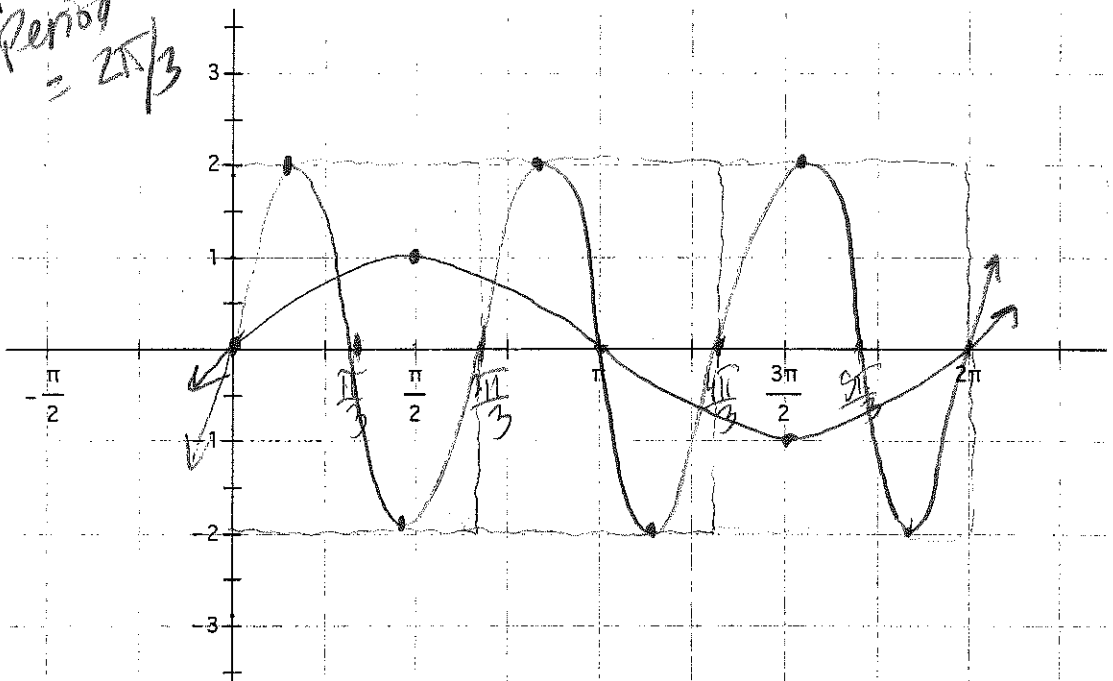
3.

a) $y = \sin x$

b) $y = 2 \sin 3x$

↑
amp = 2

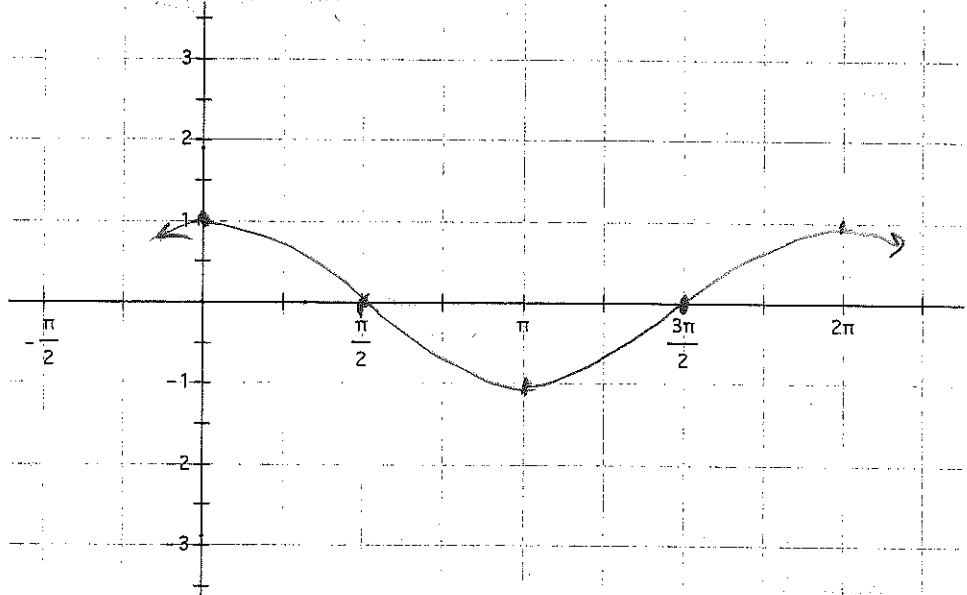
↑
Period = $\frac{2\pi}{3}$



Sections 4.5 – Graphs of Sine & Cosine Functions

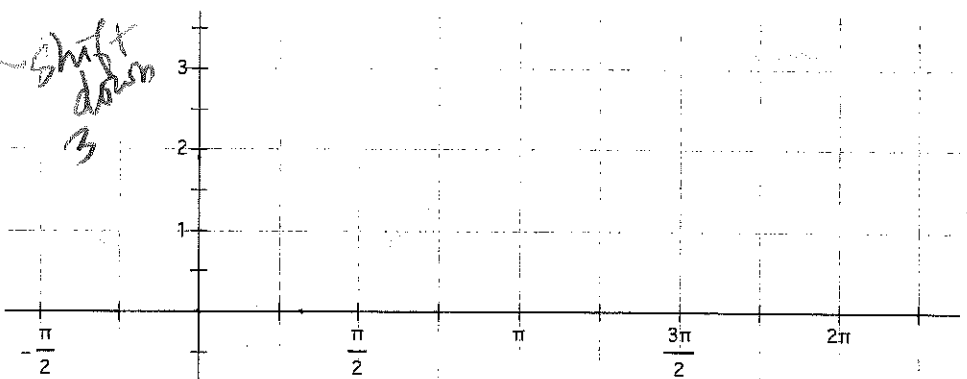
4.

a) $y = \cos x$



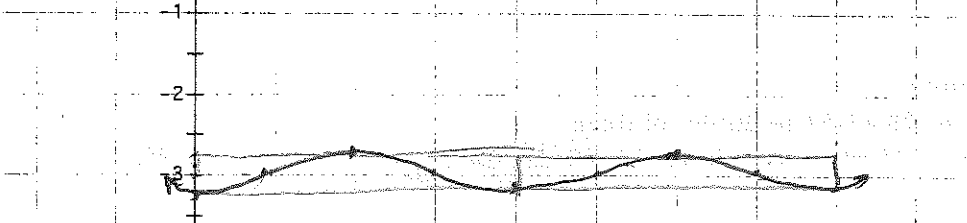
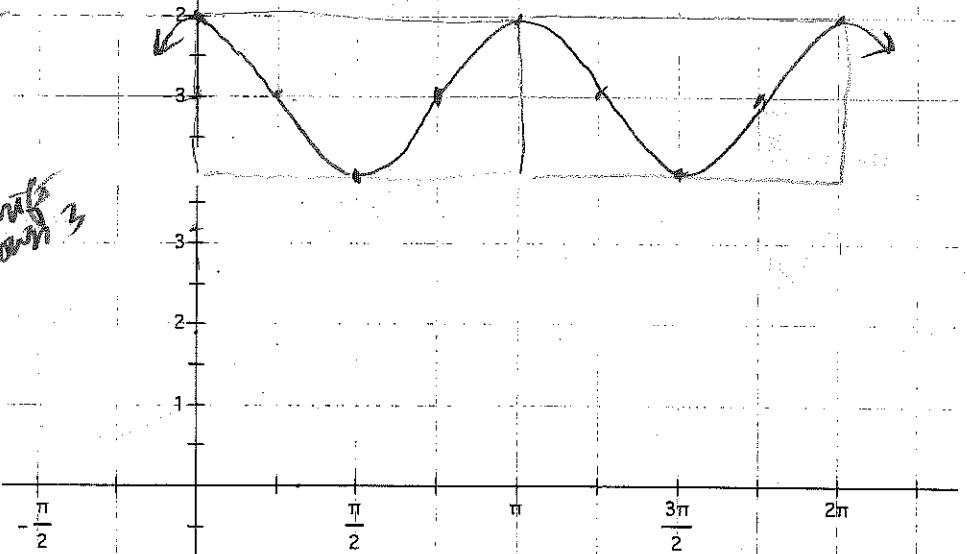
b) $y = \cos 2x - 3$

$P = \frac{2\pi}{2} = \pi$
 shift down 3



c) $y = \frac{1}{4} \cos 2x - 3$

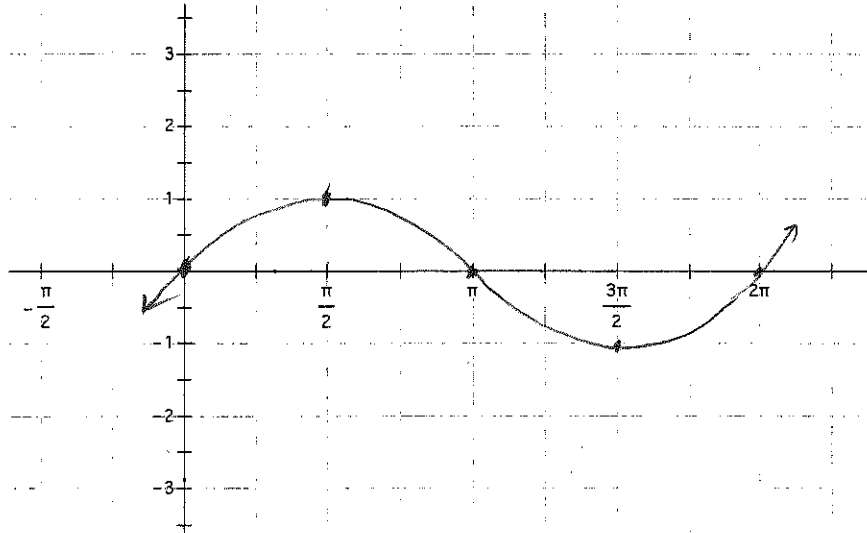
$P = \frac{2\pi}{2} = \pi$
 reflect over x-axis
 shift down 3
 Amplitude = $\frac{1}{4}$



Sections 4.5 – Graphs of Sine & Cosine Functions

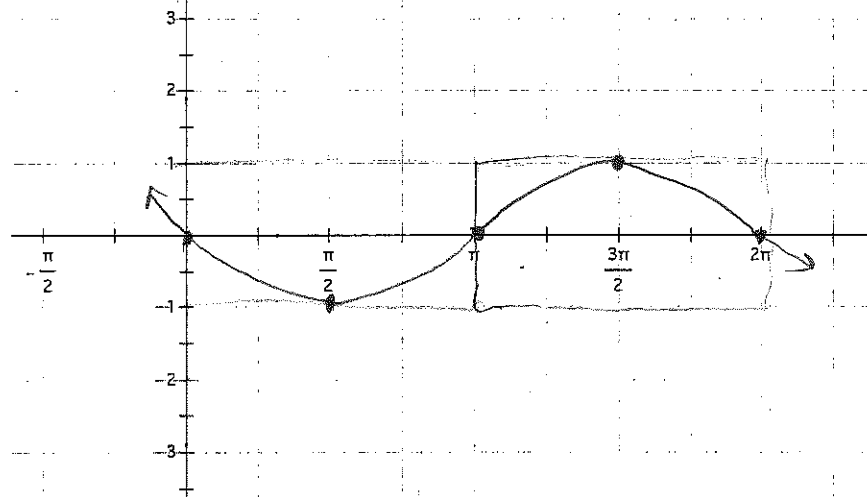
5.

a) $y = \sin x$



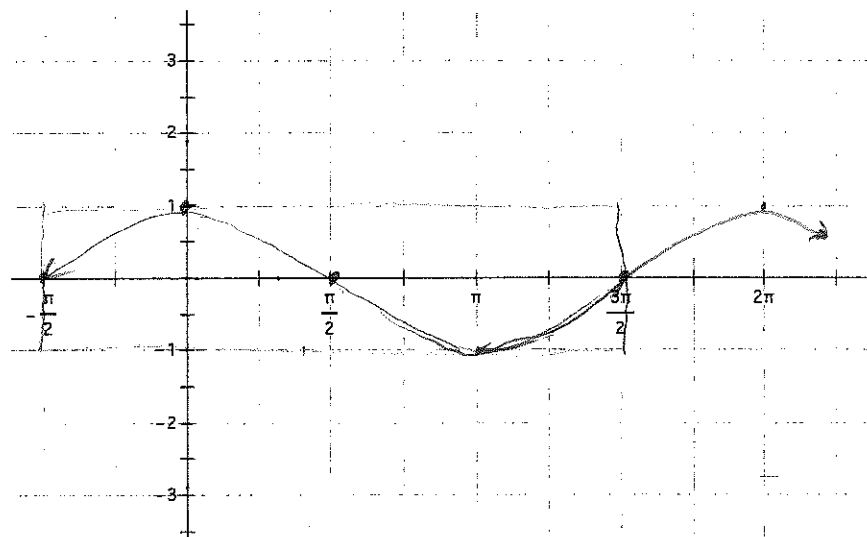
b) $y = \sin(x - \pi)$

right π



c) $y = \sin\left(x + \frac{\pi}{2}\right)$

left $\frac{\pi}{2}$



Homework

Day 1 p.328 #3-54 multiples of three

Day 2 p. 328 #4, 7, 10, 13, 16, 19, 22, 25, 28, 31, 34, 37, 40, 43, 46, 49, 52