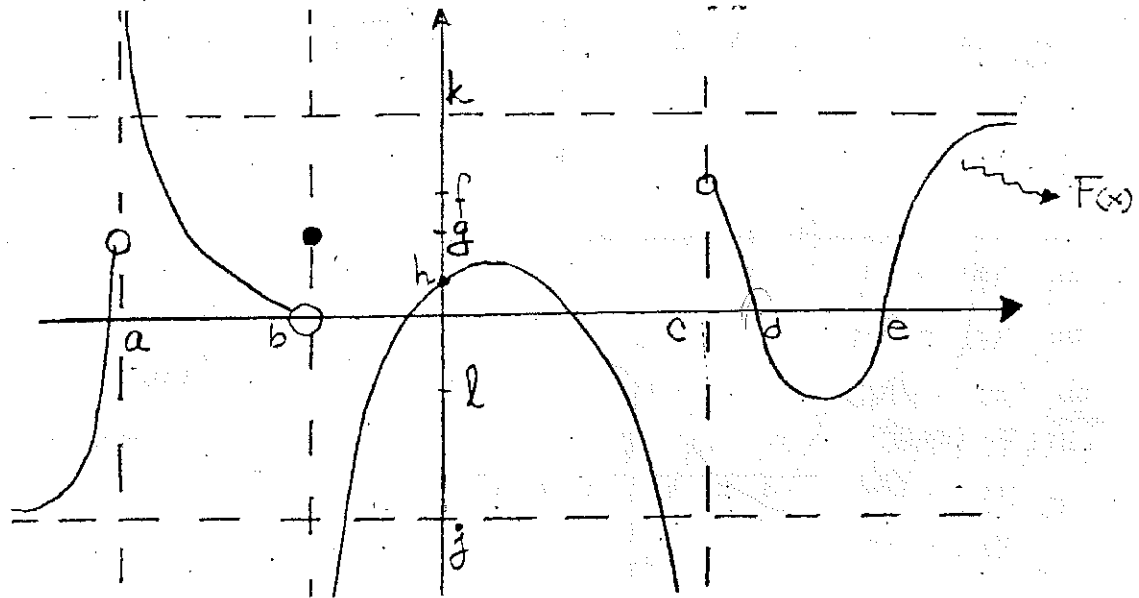


Determining Limits Visually:

Your goal is to determine the y-value that the graph is trying to reach.

- If there is a hole, the limit DOES exist, and is the y-value of that hole.
- If there is a vertical asymptote, the limit may be $\pm\infty$, or may be DNE; you have to look to find out.
- If there is a jump, you must look at the one-sided limits, and again, the limit may be DNE.

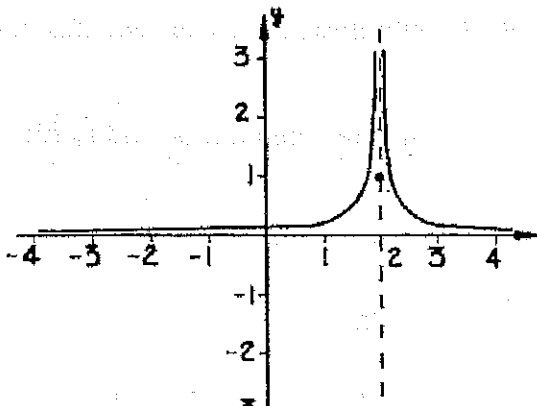


- | | | |
|--|---|---|
| 1. $\lim_{x \rightarrow \infty} F(x) = k$ | 2. $\lim_{x \rightarrow -\infty} F(x) = j$ | 3. $\lim_{x \rightarrow a^+} F(x) = \infty$ |
| 4. $\lim_{x \rightarrow a^-} F(x) = g$ | 5. $\lim_{x \rightarrow a} F(x) = \text{DNE}$ | 6. $\lim_{x \rightarrow 0} F(x) = h$ |
| 7. $\lim_{x \rightarrow b^+} F(x) = -\infty$ | 8. $\lim_{x \rightarrow b^-} F(x) = 0$ | 9. $\lim_{x \rightarrow b} F(x) = \text{DNE}$ |
| 10. $\lim_{x \rightarrow c} F(x) = \text{DNE}$ | 11. $\lim_{x \rightarrow d} F(x) = 0$ | 12. $\lim_{x \rightarrow e} F(x) = 0$ |
| 13. $F(e) = 0$ | 14. $F(0) = h$ | 15. $F(b) = g$ |

More examples:

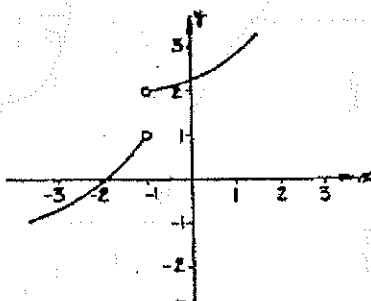
For the function f graphed to the right, find

- (a) $\lim_{x \rightarrow 2^-} f(x) = \infty$
- (b) $\lim_{x \rightarrow 2^+} f(x) = \infty$
- (c) $\lim_{x \rightarrow 2} f(x) = \infty$
- (d) $f(2) = 1$
- (e) $\lim_{x \rightarrow -\infty} f(x) = 0$
- (f) $\lim_{x \rightarrow +\infty} f(x) = 0$



For the function f graphed to the right, find

- (a) $\lim_{x \rightarrow -1^-} f(x) = 1$
- (b) $\lim_{x \rightarrow -1^+} f(x) = 2$
- (c) $\lim_{x \rightarrow -1} f(x) = \text{DNE}$
- (d) $f(-1) = \text{DNE}$
- (e) $\lim_{x \rightarrow +\infty} f(x) = \infty$
- (f) $\lim_{x \rightarrow -\infty} f(x) = -\infty$



For the function f graphed to the right, find

- (a) $\lim_{x \rightarrow 2^-} f(x) = 1$
- (b) $\lim_{x \rightarrow 2^+} f(x) = 2$
- (c) $\lim_{x \rightarrow 2} f(x) = 1$
- (d) $f(2) = 2$
- (e) $\lim_{x \rightarrow 0^+} f(x) = +\infty$
- (f) $\lim_{x \rightarrow +\infty} f(x) = 0$

